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DES SCIENCES  
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# Ultracold molecules, from dilute to quantum degenerate gases

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Laboratoire interdisciplinaire Carnot de Bourgogne

Winter school – Physics and Mathematics of Bose-Einstein Condensates

25<sup>th</sup> of February 2025

# Outline

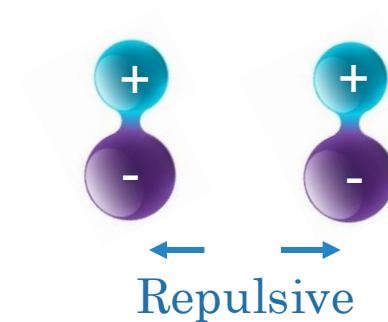
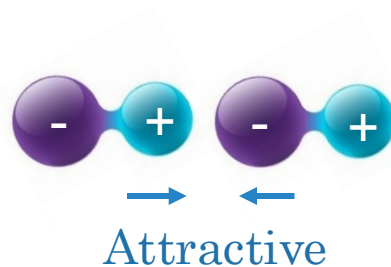
- Introduction: System – Goal – Applications.
- Planning a BEC of ground state molecules
- Dealing with losses: Shielding of collisions
- Results and First observation of molecular BEC

# Introduction: system

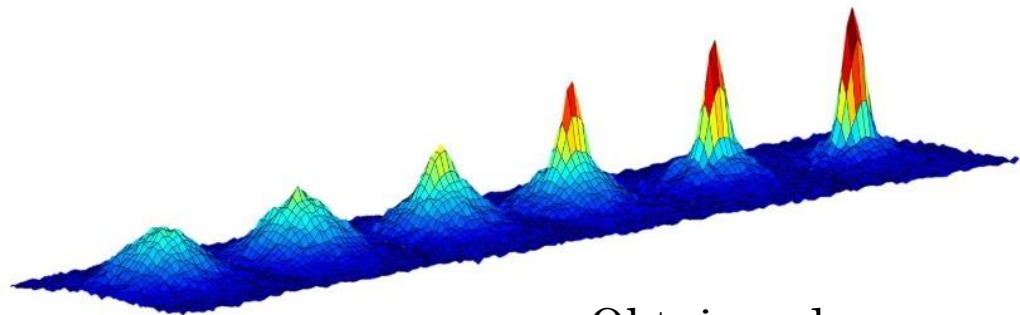
3	6.941
<b>Li</b>	
LITHIUM	
11	22.990
<b>Na</b>	
SODIUM	
19	39.098
<b>K</b>	
POTASSIUM	
37	85.468
<b>Rb</b>	
RUBIDIUM	
55	132.91
<b>Cs</b>	
CÉSIUM	

Polar bi-alkali metal ultracold molecules:

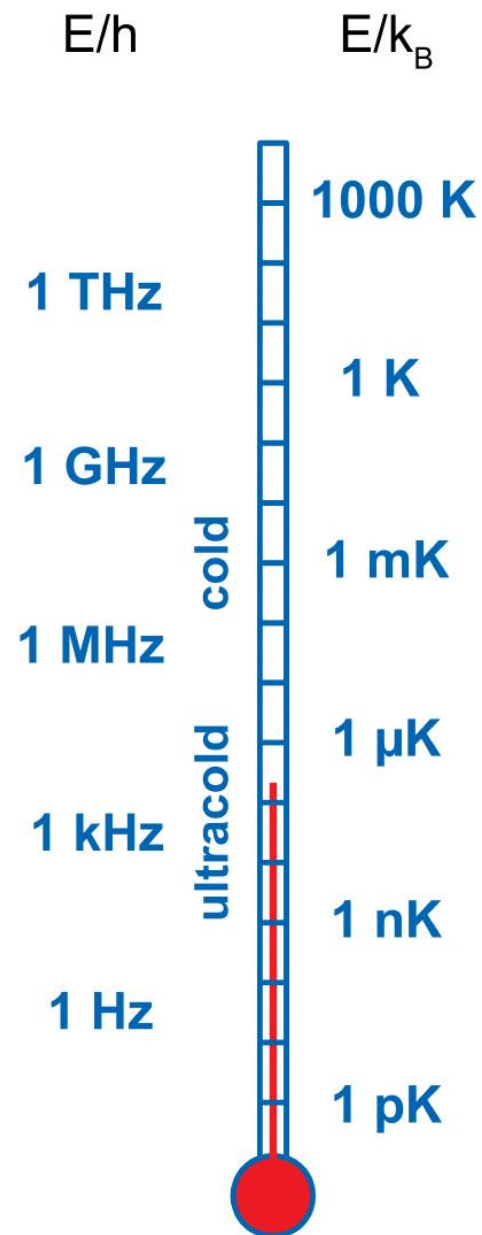
- Strong permanent electric dipole moment  
(body fixed frame)
- Easily manipulated by external electric fields
- Long range anisotropic interactions:  
dipole-dipole interaction (DDI)



# Introduction: Goal



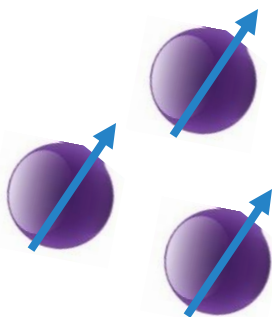
Obtain a dense gas ( $10^{12} - 10^{15} \text{ cm}^{-3}$ )  
of polar ultracold molecules ( $\ll 1 \text{ mK}$ )  
in their **absolute ground state**.  
Aiming to reach **quantum degeneracy**.



# Introduction: Cold dipolar systems

Dipole moment

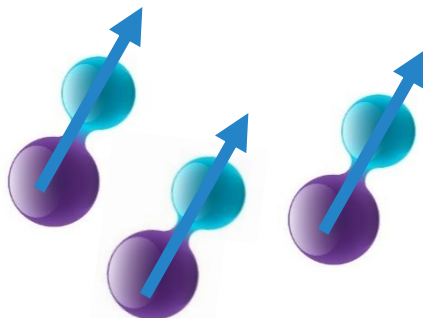
Magnetic Atoms



e.g.: Cr, Er, Dy, etc...

Long-lived, very cold,  
Weaker dipole moment

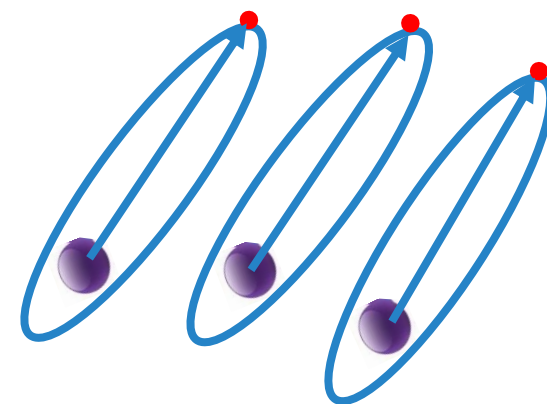
Ultracold Polar Molecules



e.g.: NaK, NaRb, NaCs, RbCs,  
SrF, BaF, YO, CaOH, etc...

Intermediate lifetime  
Intermediate to Strong dipole moment

Rydberg Atoms



Short lifetime  
Strong dipole moment,

Lifetime

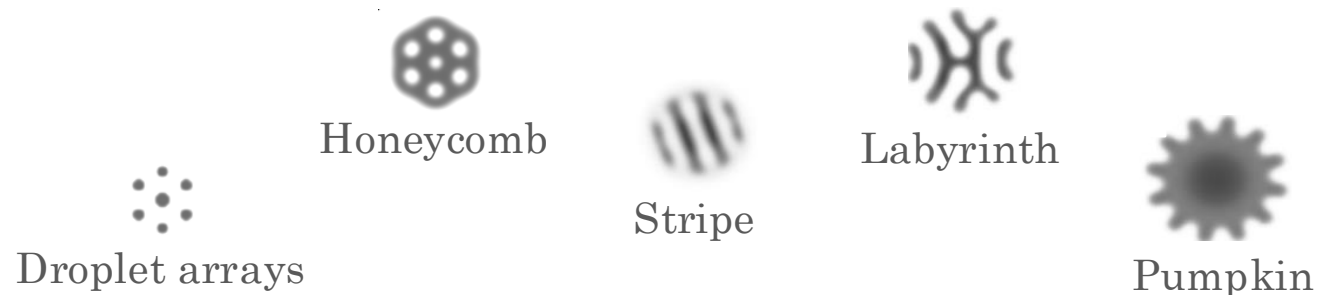
# Introduction: Applications

Molecular quantum degenerate gases bring many of the theoretical predictions on dipolar gases into experimental reach

Macroscopic manifestation of microscopic anisotropic interactions

- Simulation of **condensed matter** systems.
- Transitions to a variety of **exotic supersolid states**.

Supersolid states of trapped molecular BECs

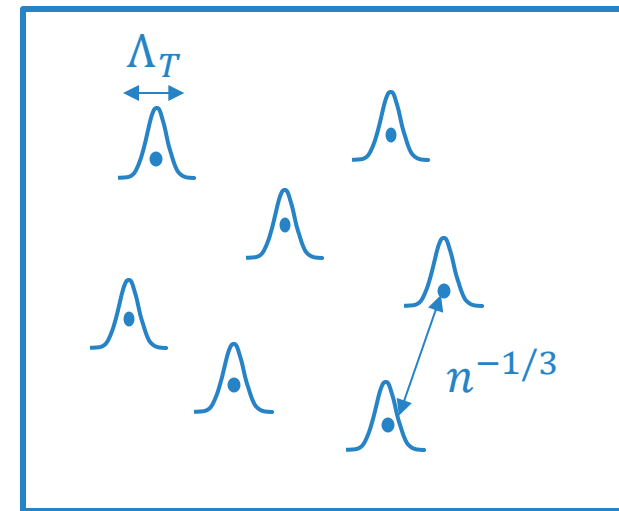


Schmidt *et al* PRR4,013235 (2022)

# Introduction: Reminder on degenerate gases: $n \Lambda_T^3 \approx 1$

What do we need to reach quantum degeneracy?

$$\Lambda_T \propto 1/\sqrt{T}$$



Classical regime  
(dilute gas)

$$\Lambda_T = \sqrt{\frac{2\pi\hbar^2}{mk_B T}} \equiv \text{De Broglie wavelength}$$

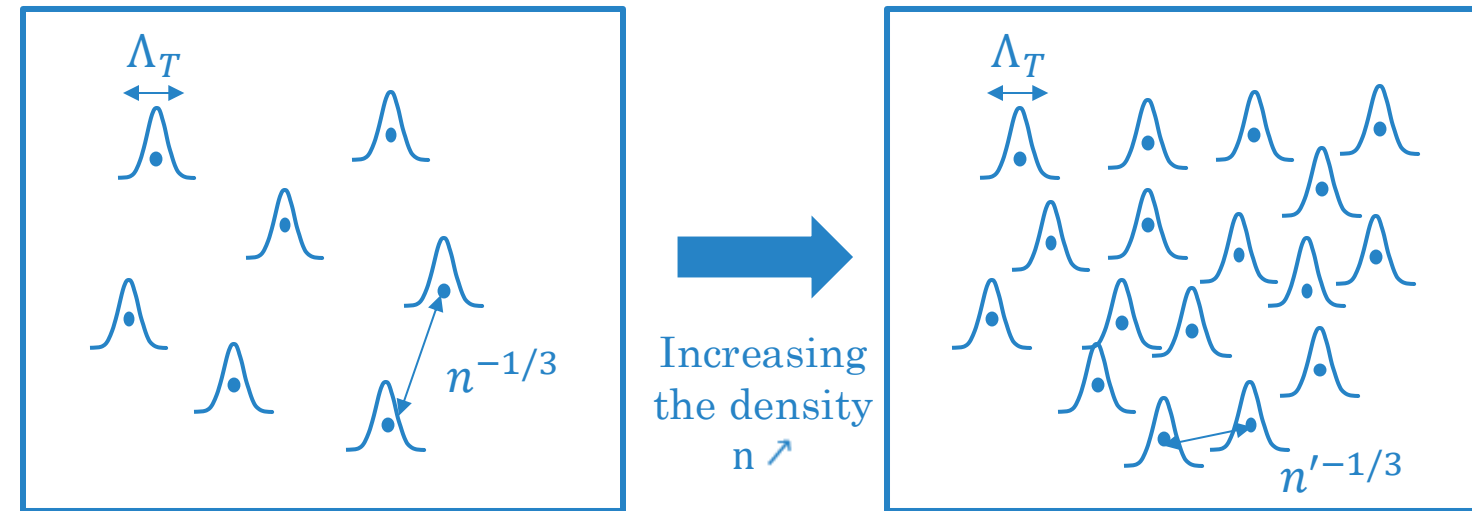
$T \equiv$  gas temperature

$$n = \frac{N}{V} \equiv \text{gas density}$$

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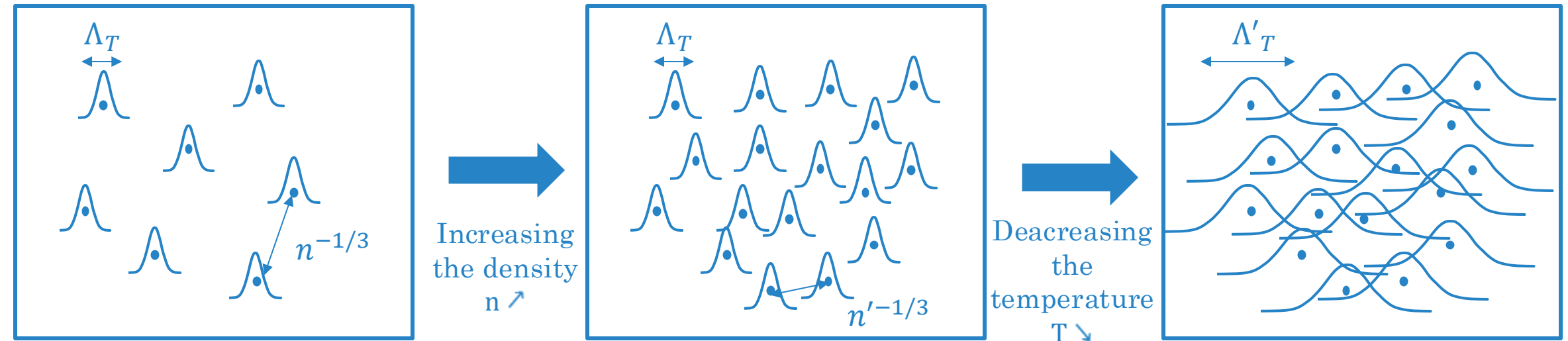
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Classical regime  
(dilute gas)

Quantum regime  
(correlated gas)

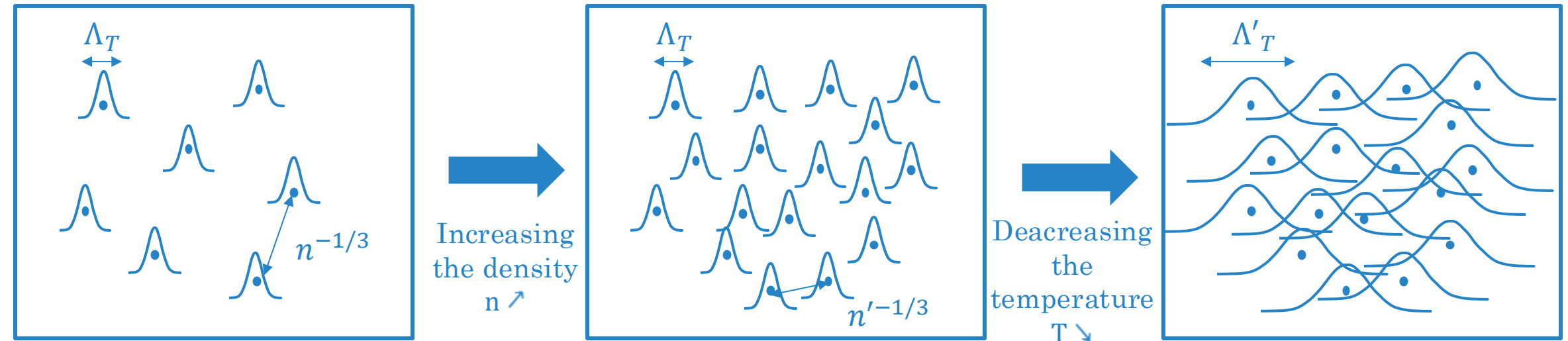
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# Introduction: Reminder on degenerate gases: $n \Lambda_T^3 \approx 1$

What do we need to reach quantum degeneracy?



Classical regime  
(dilute gas)

Two main ingredients:  
Temperature and Density

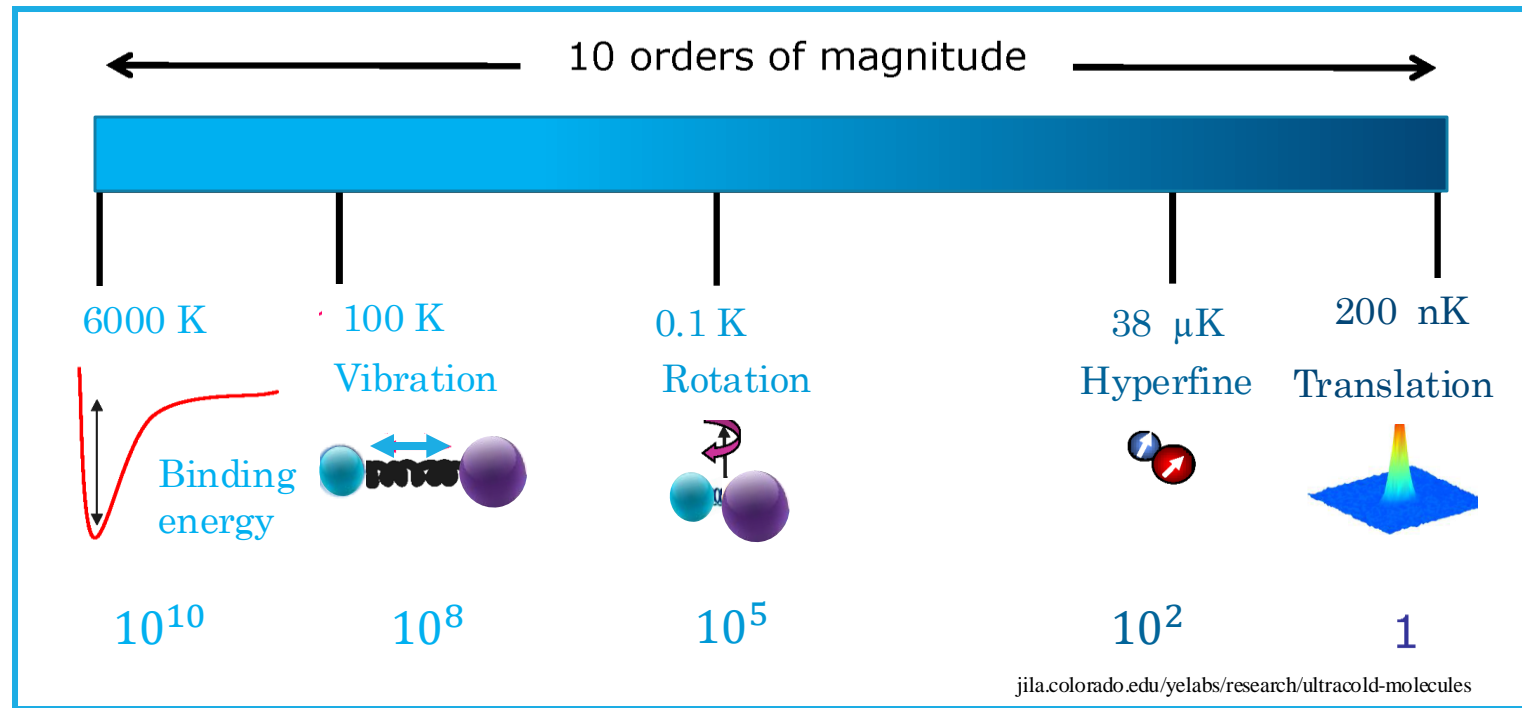
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$T \equiv$  gas temperature

$$n = \frac{N}{V} \equiv \text{gas density}$$

# Temperature/Energy orders of magnitude in bi-alkali molecules



Internal  
degrees of freedom

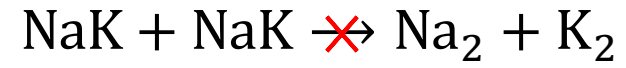
External  
degree of freedom

# Lifetime of ground state $^{23}\text{Na}^{39}\text{K}$ gas:

Density  $10^{12} \text{ cm}^{-3}$

Temperature 300 nK

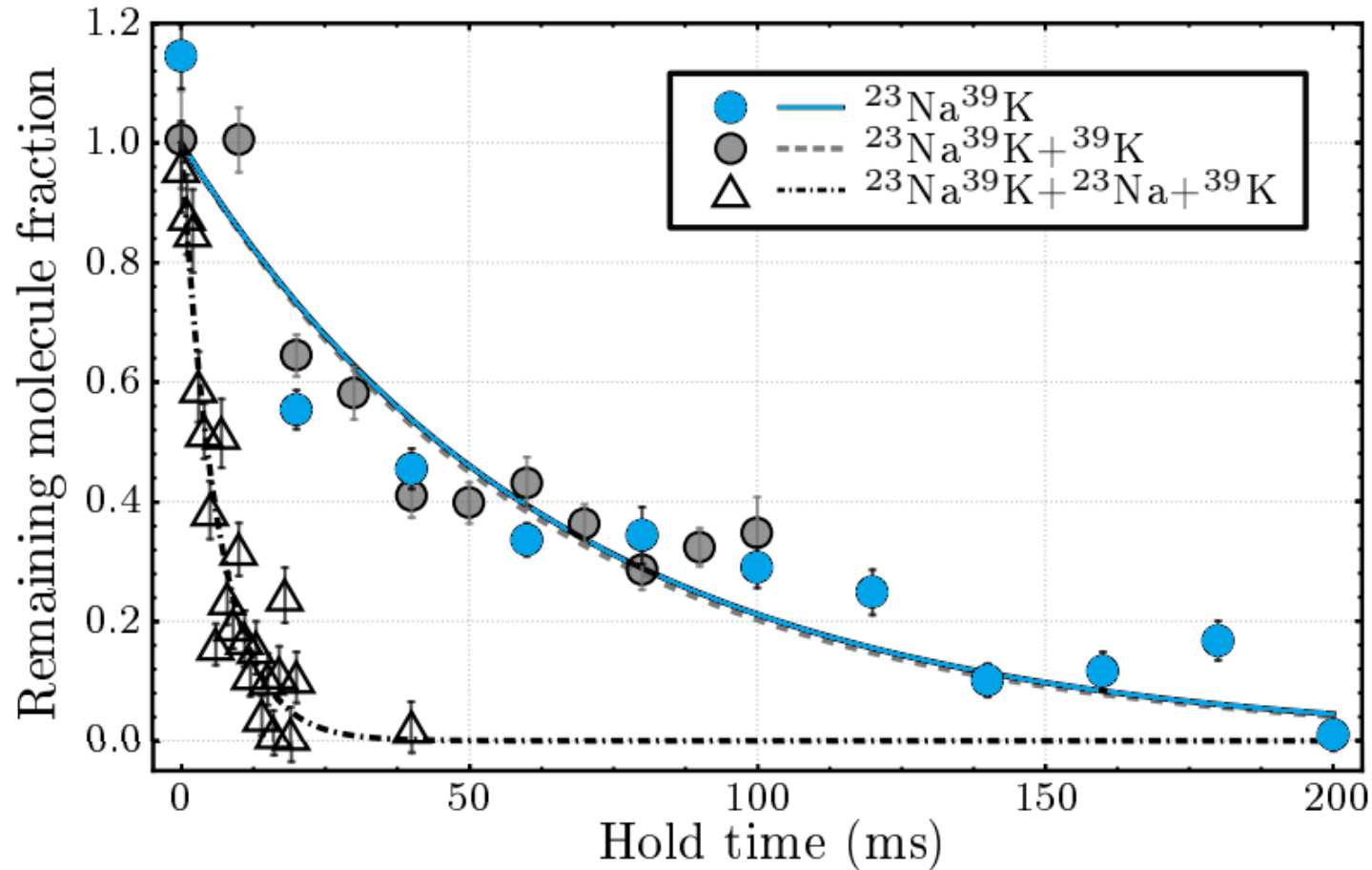
$^{23}\text{Na}^{39}\text{K}$  is **not chemically reactive**:



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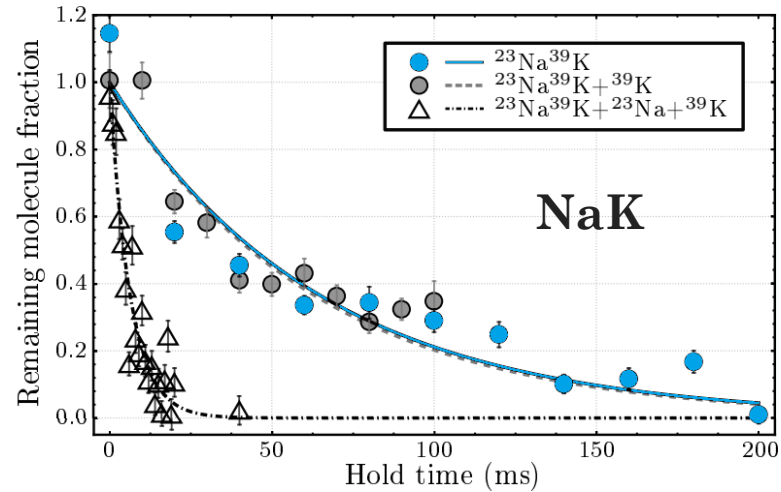
$^{23}\text{Na}^{39}\text{K}$  is **not chemically reactive**:  
 $\text{NaK} + \text{NaK} \not\rightarrow \text{Na}_2 + \text{K}_2$



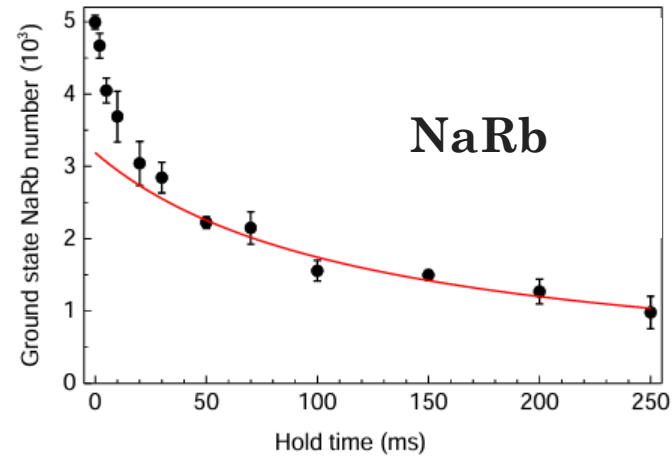
Loss rate:  
 $4.49 (\pm 1.18) \times 10^{-10} \text{ cm}^3 \text{ s}^{-1}$

Hannover  
PRL 125, 083401 (2020)

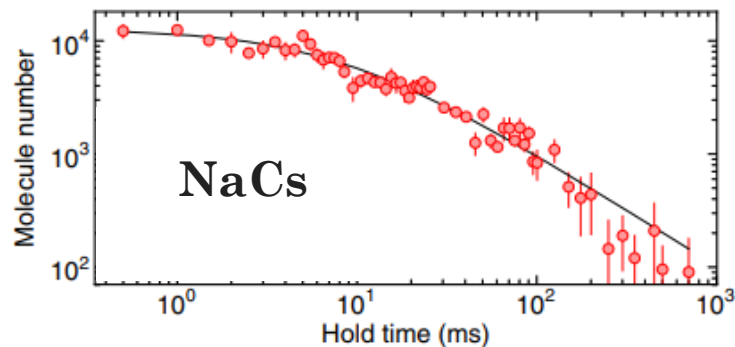
# Not only $^{23}\text{Na}^{39}\text{K}$ gas:



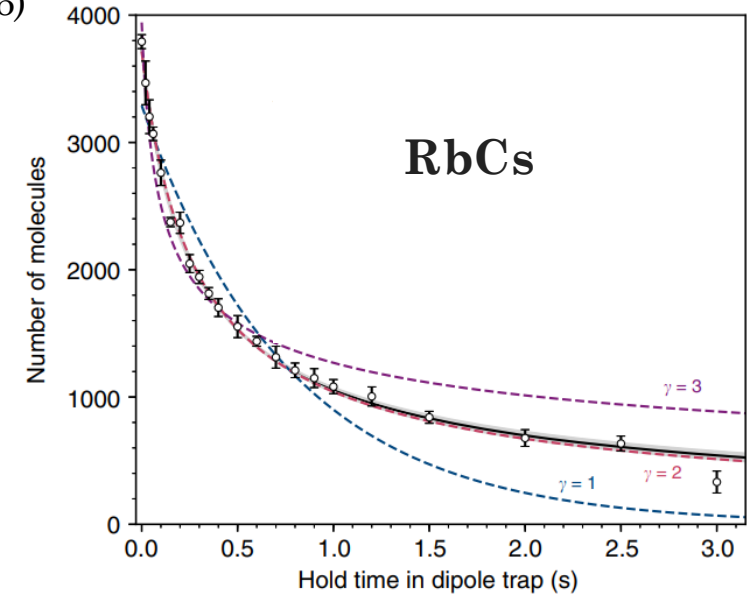
Hannover  
PRA 101, 042704 (2020)



Hong Kong  
PRL 116, 205303 (2016)



Columbia U  
PRL 130, 113002 (2023)



Durham  
Nature commun 10, 3104 (2019)

Consequence: the **density decreases** preventing the formation of a degenerate gas...



# Shielding collisions



# Shielding



Engineering the long-range interaction  
between ultracold molecules  
using external fields:

Changing **attractive** interactions into **repulsive** ones

→ Shield the collisions

→ Prevent the loss.





# Shielding

Theoretical Proposals:



Static electric field

Avdeenkov *et al* PRA 73 022707 (2006)  
Wang *et al* New J.Phys 17 035015 (2015)

Experimental validation:



On fermionic KRb  
For  $E = 12$  kV/cm

Li *et al* Nature Phys. 17, 1144 (2021)

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X.Tie *et al* PRL 125, 153202 (2020)

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X.Tie *et al* PRL 125, 153202 (2020)

→ Two-photon Optical field

Charbel Karam *et al.* PRR 5 033074 (2023)

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In progress  
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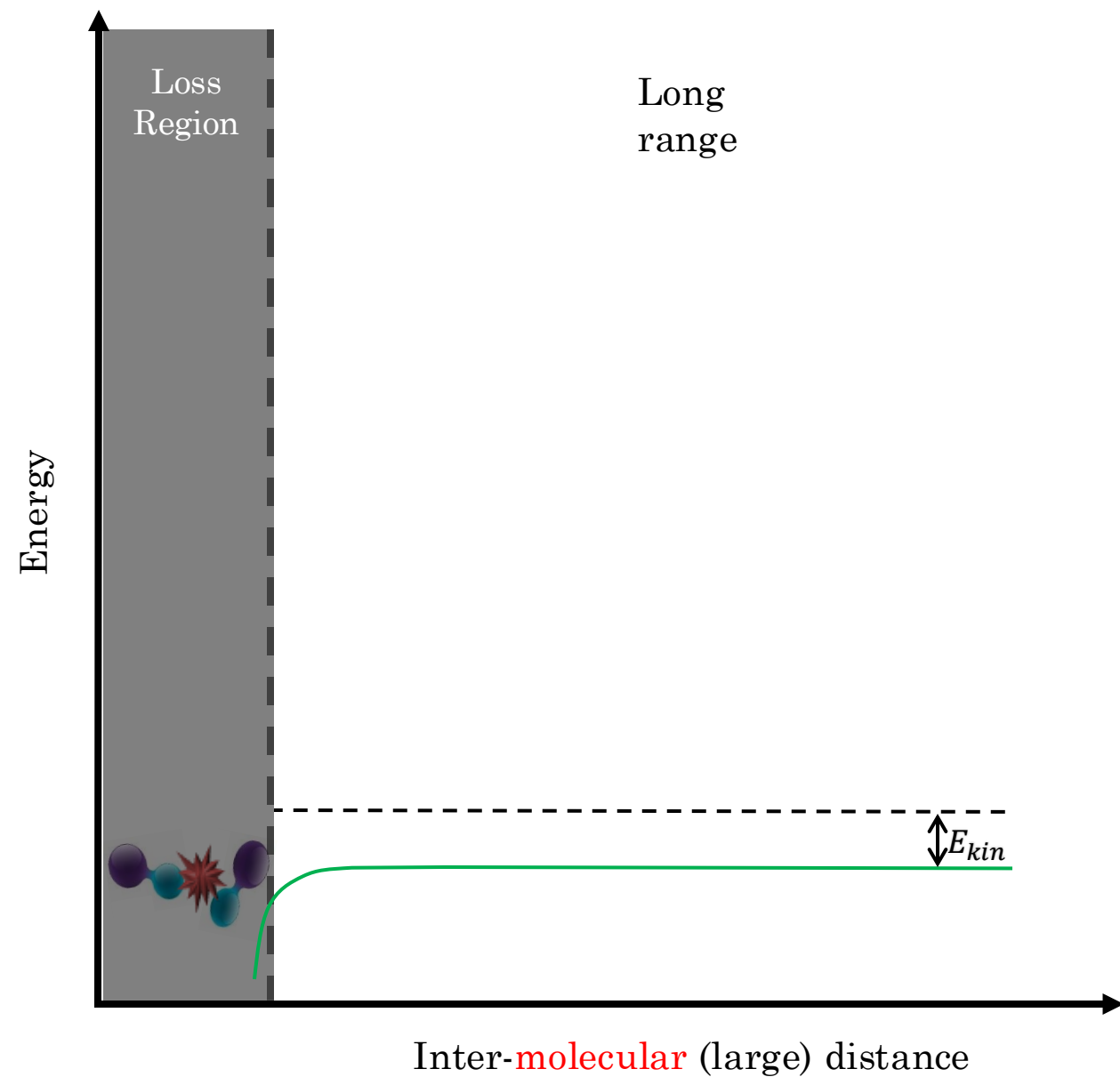
→

In progress  
on bosonic NaK

Degenerate  
Fermi Gas

First BEC  
of ground state  
dipolar molecules

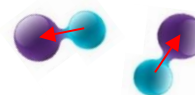
# How to shield ?



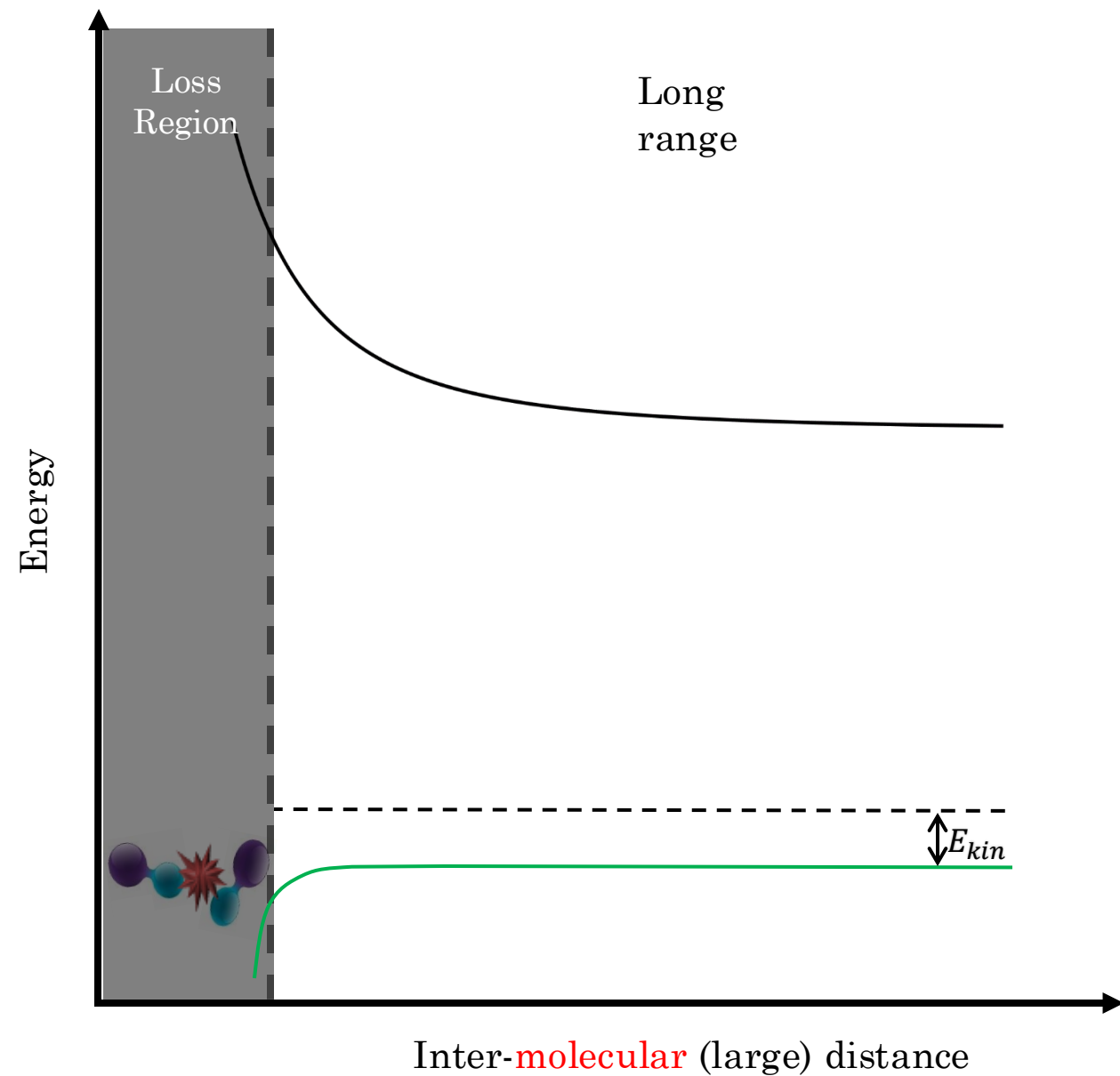
$$\hat{H} = \hat{T} + \frac{\hat{L}^2}{2\mu R^2} + \hat{H}_{rot} + \hat{V}_{mol-mol}(R)$$

Mainly anisotropic  
dipole-dipole interaction  
 $\propto \frac{1}{R^3}$ .

Ground + Ground



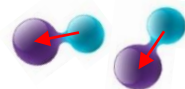
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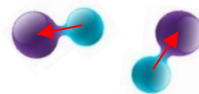
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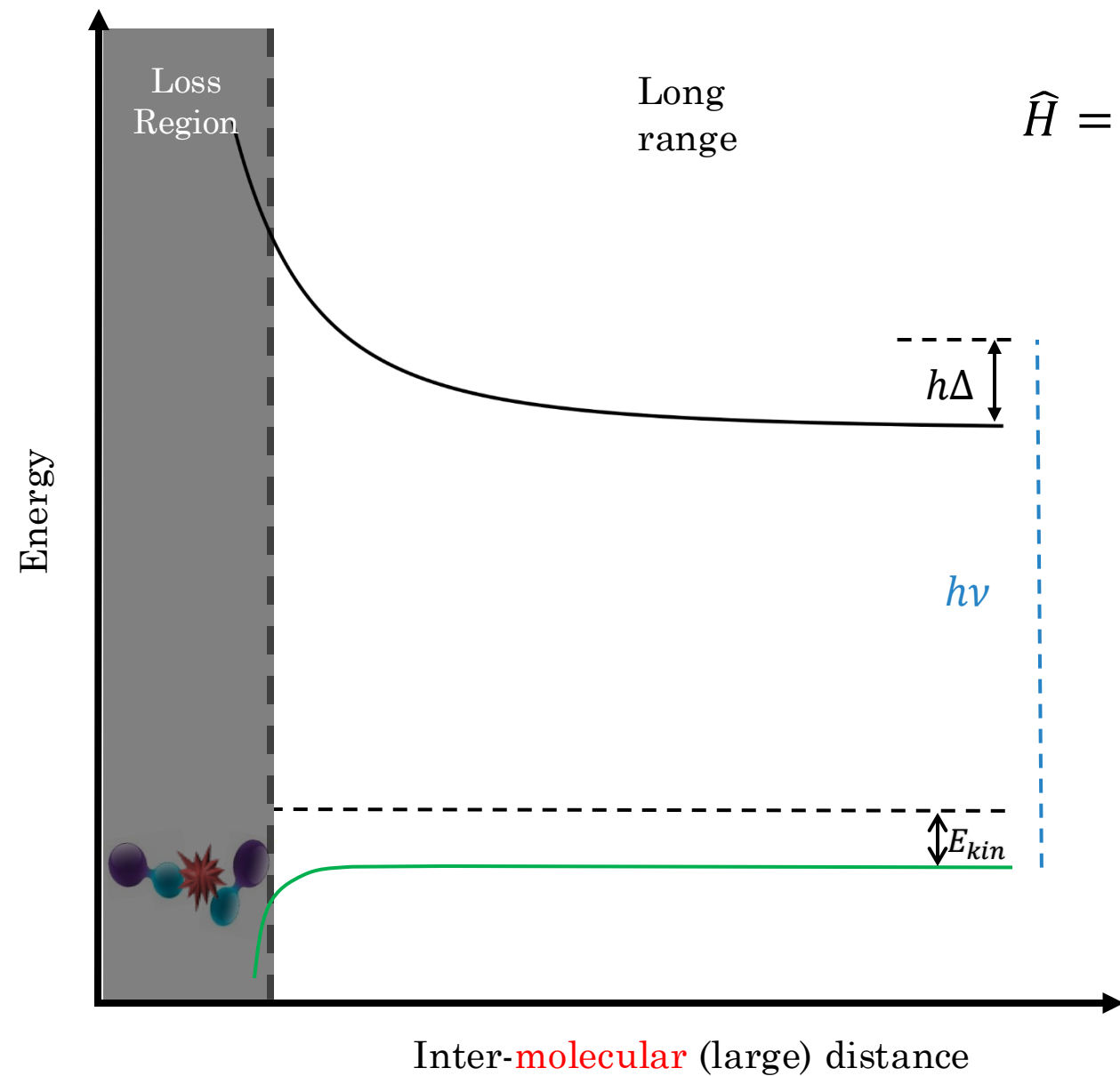
Ground + Excited



Ground + Ground



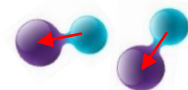
# How to shield ?



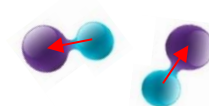
$$\hat{H} = \hat{T} + \frac{\hat{L}^2}{2\mu R^2} + \hat{H}_{rot} + \hat{V}_{mol-mol}(R) + \hat{H}_f$$

$$\hbar\omega \left( \hat{a}^\dagger \hat{a} + \frac{1}{2} \right)$$

Ground + Excited



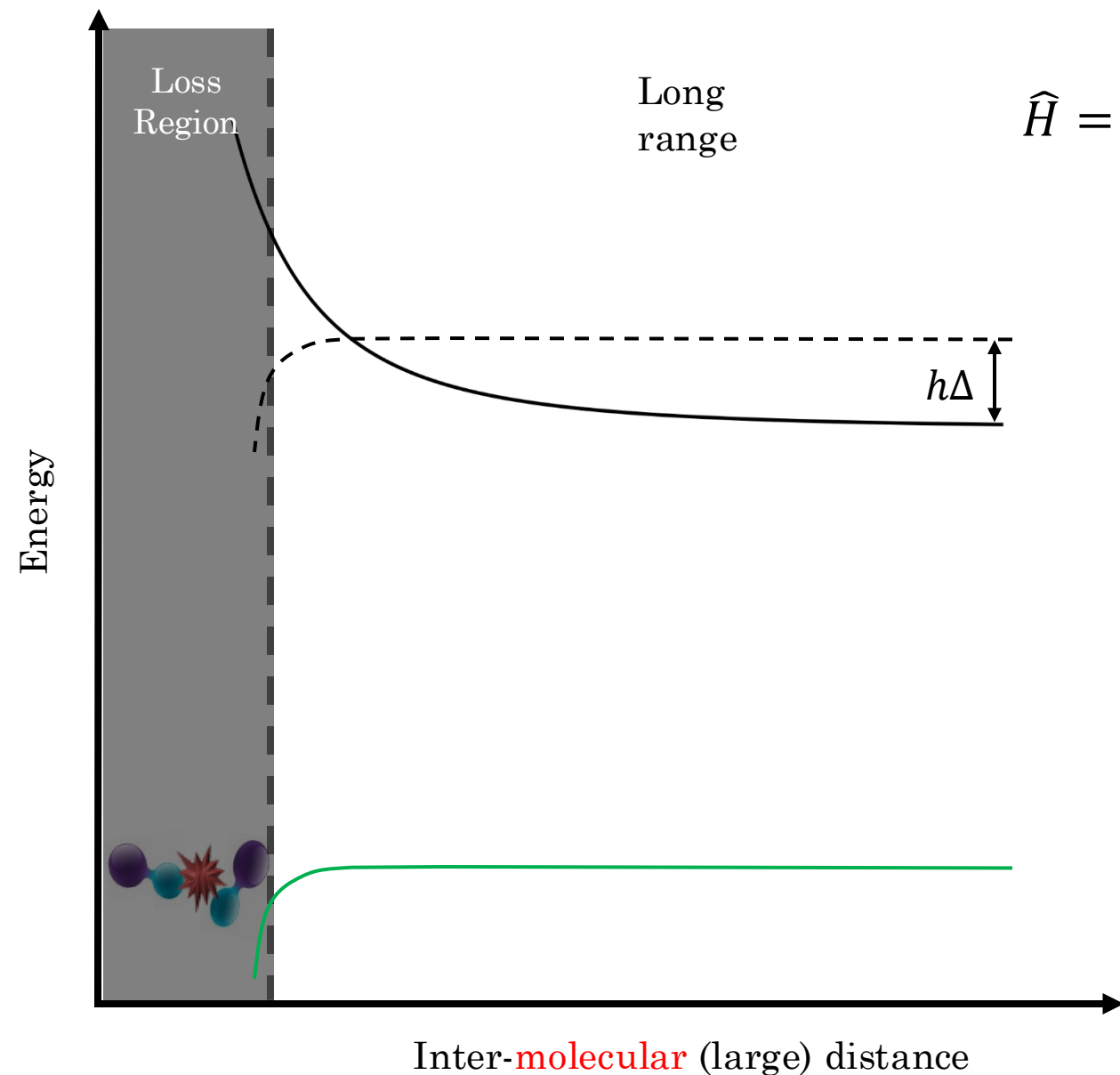
Ground + Ground



We **couple** the ground state to a repulsive excited state using a **blue detuned photon** by respect to the transition.



# How to shield ?



$$\hat{H} = \hat{T} + \frac{\hat{L}^2}{2\mu R^2} + \hat{H}_{rot} + \hat{V}_{mol-mol}(R) + \hat{H}_f$$

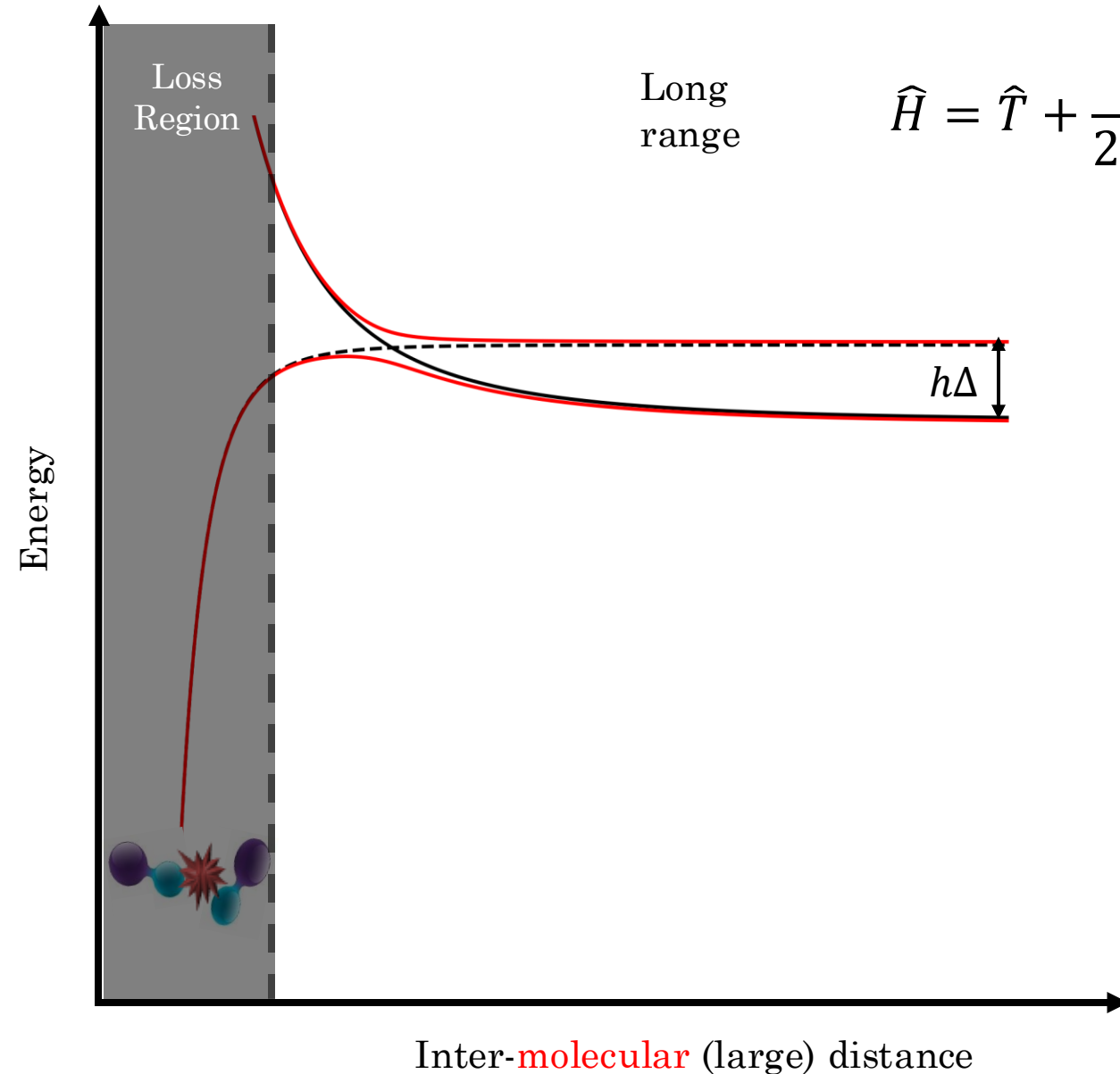
Ground + Ground + 1 photon

Ground + Excited

$$\hbar\omega \left( \hat{a}^\dagger \hat{a} + \frac{1}{2} \right)$$

We **couple** the ground state to a repulsive excited state using a **blue detuned photon** by respect to the transition.

# How to shield ?



Long  
range

$$\hat{H} = \hat{T} + \frac{\hat{L}^2}{2\mu R^2} + \hat{H}_{rot} + \hat{V}_{mol-mol}(R) + \hat{H}_f + \boxed{\hat{H}_I}$$

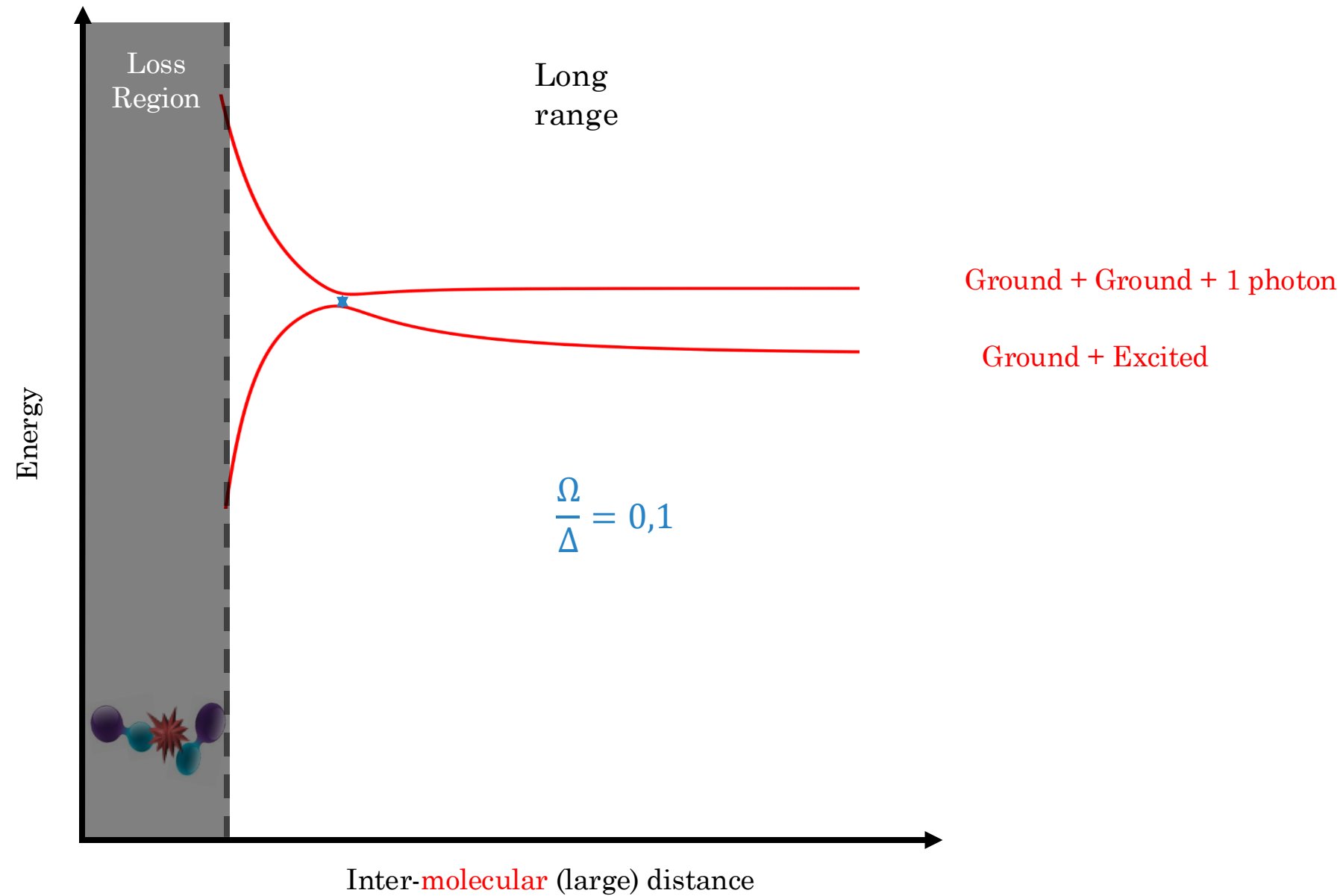
↓  
 $-\vec{d} \cdot \vec{E}(t)$

Ground + Ground + 1 photon

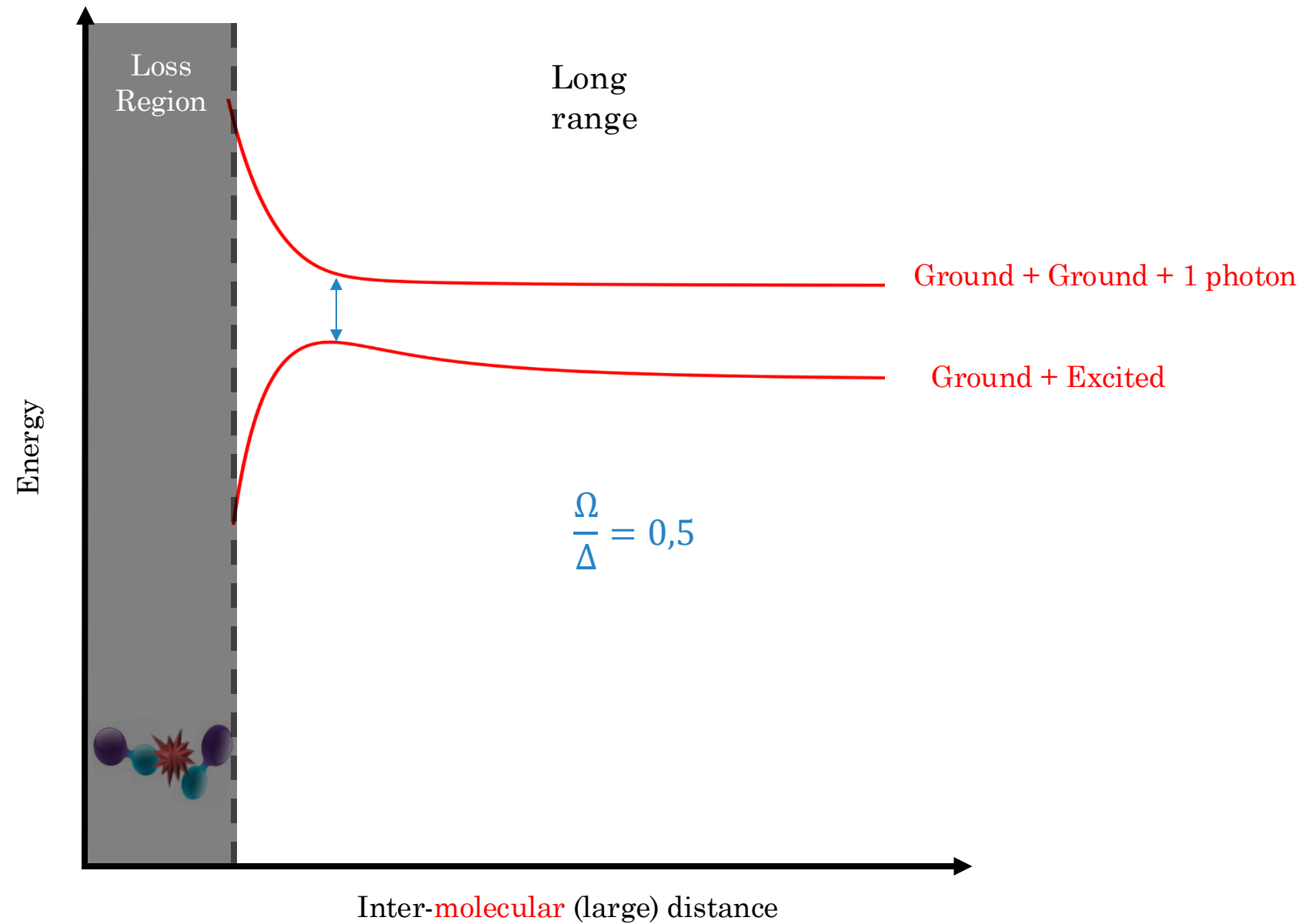
Ground + Excited

Crossing → **Avoided crossing**  
 Dependent on light parameters:  
 - Detuning  $\Delta$   
 - Rabi frequency  $\Omega \propto \sqrt{I}$

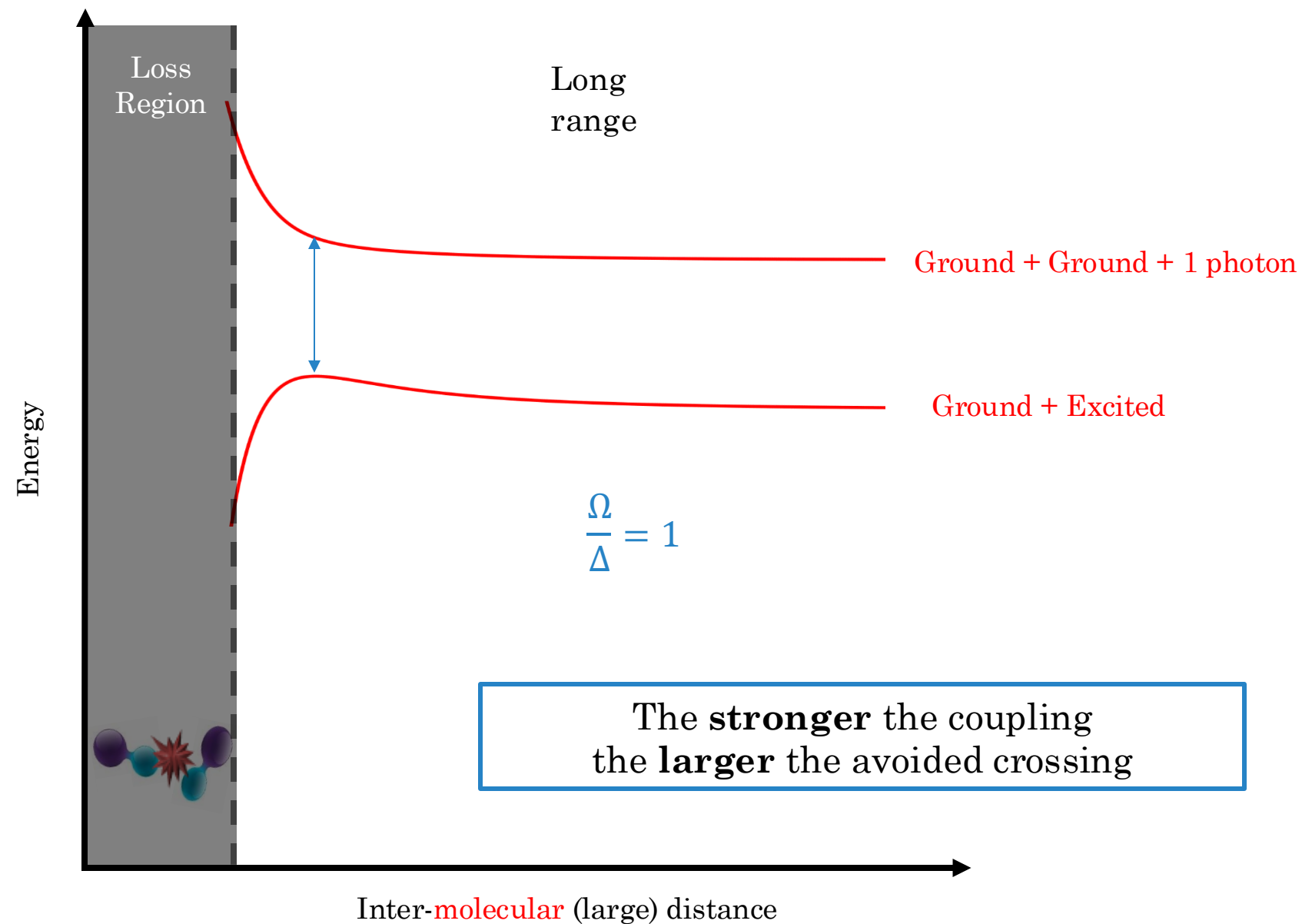
# How to shield: Dependency on light parameters



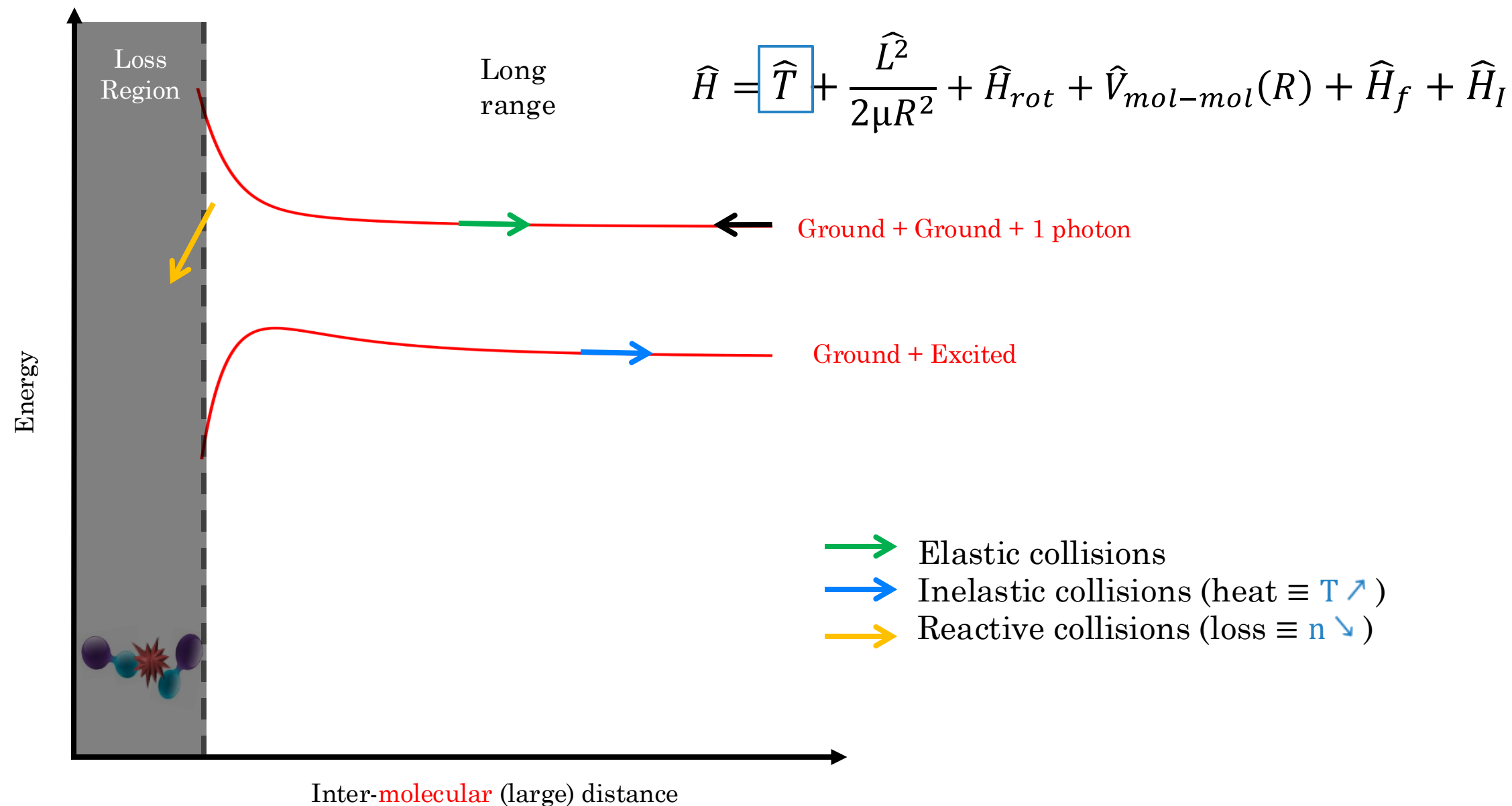
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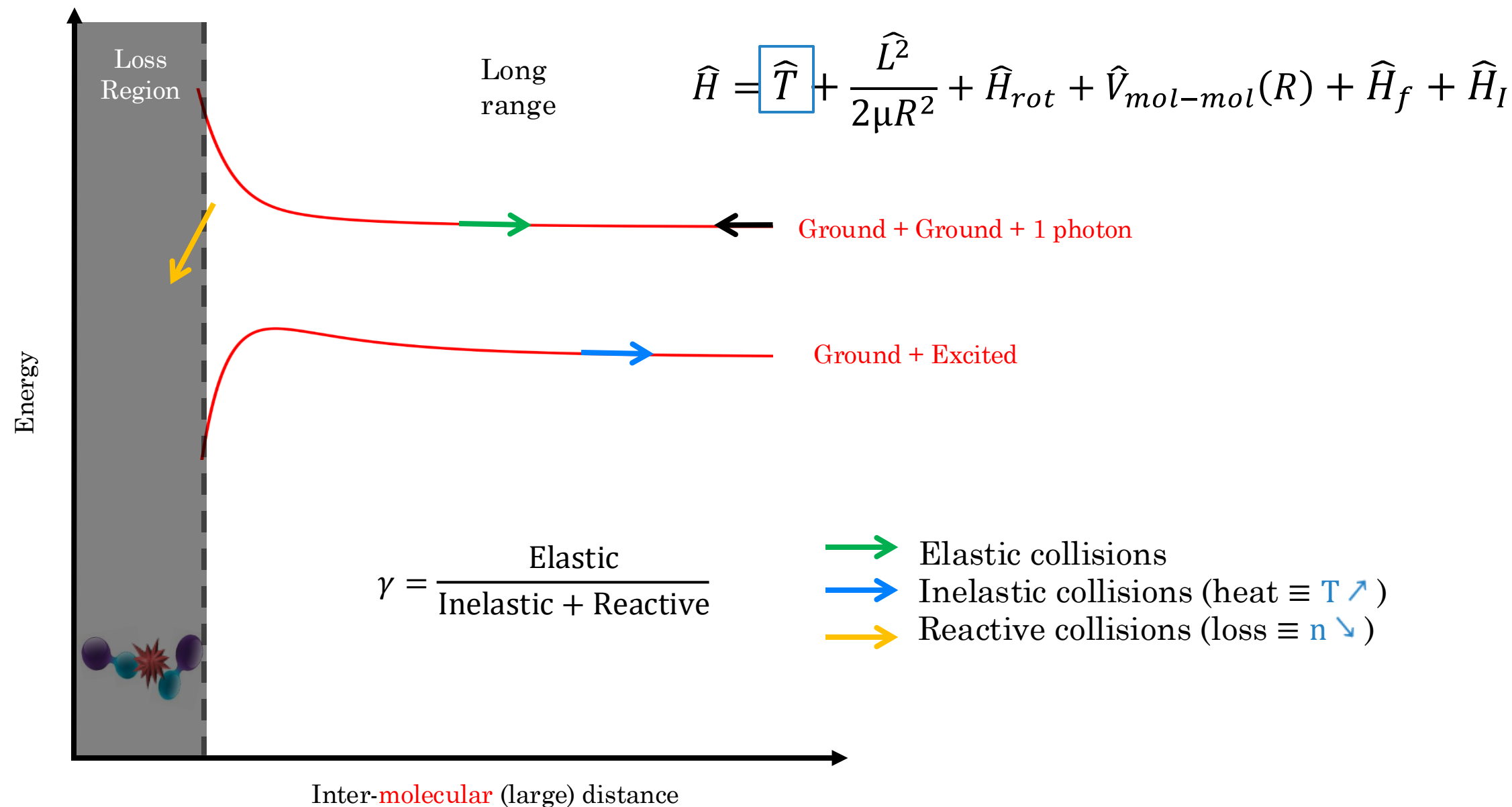
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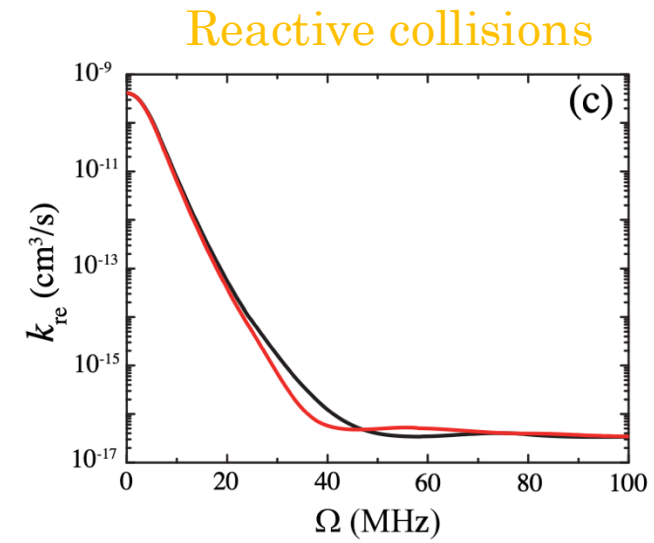
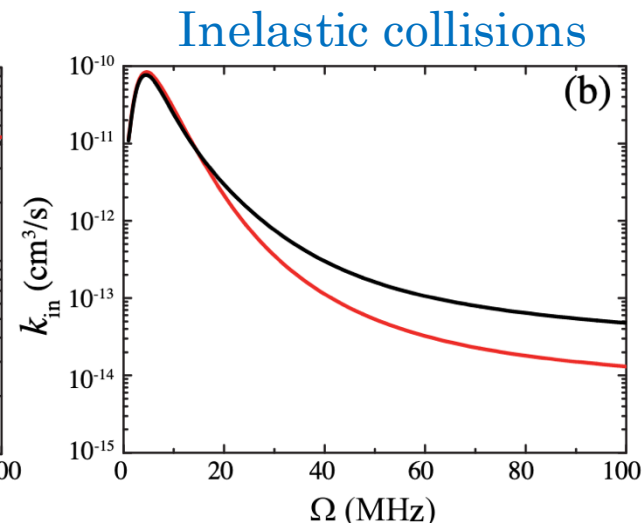
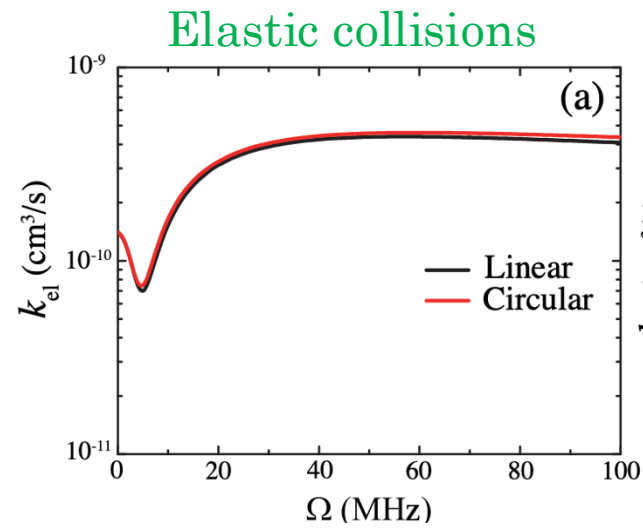
# How to shield: Dynamics and collision rates



# How to shield: Dynamics and collision rates



# Results: Optical shielding



X.Tie *et al* PRL 125, 153202 (2020)



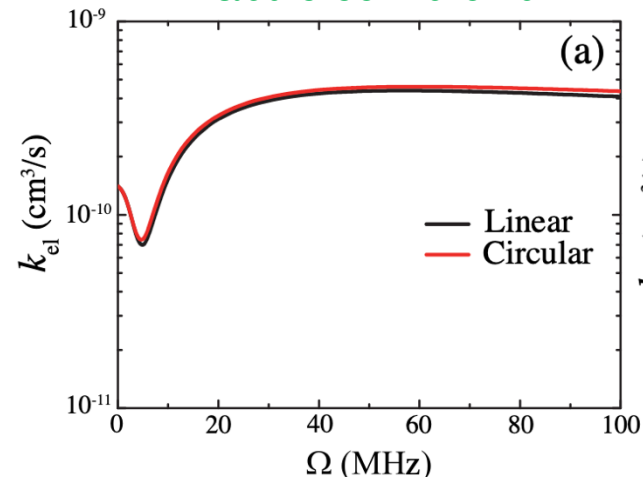
# Results: Optical shielding

Higher elastic  
collision rate

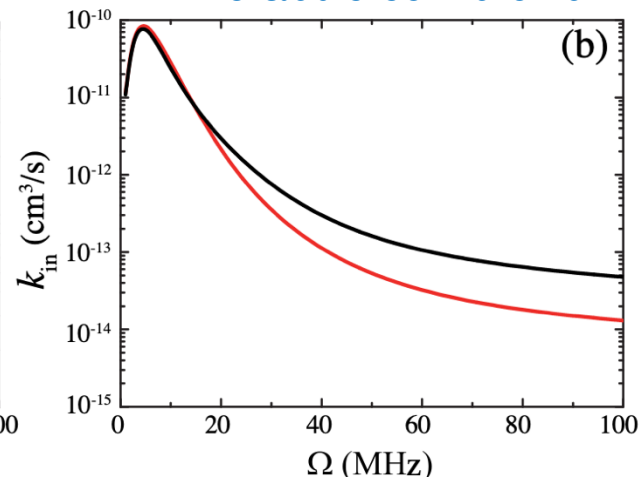
No additional heating

Low losses

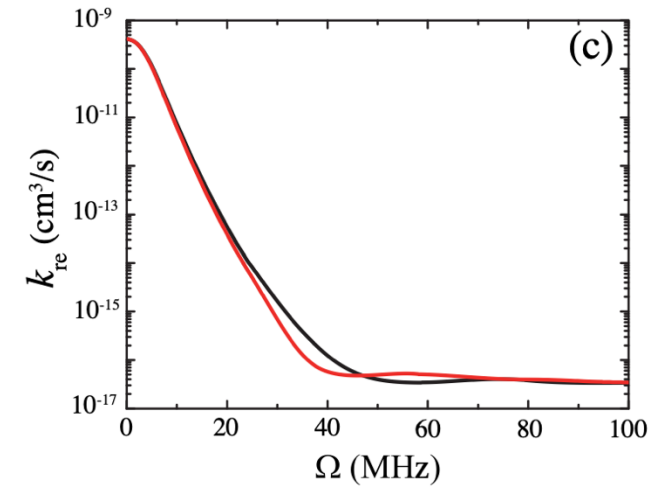
Elastic collisions



Inelastic collisions

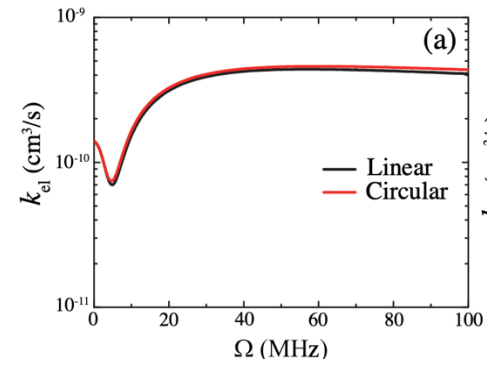


Reactive collisions

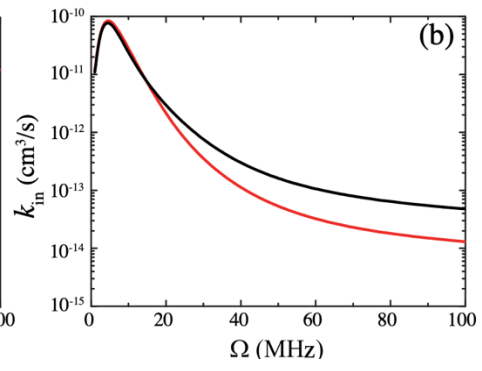


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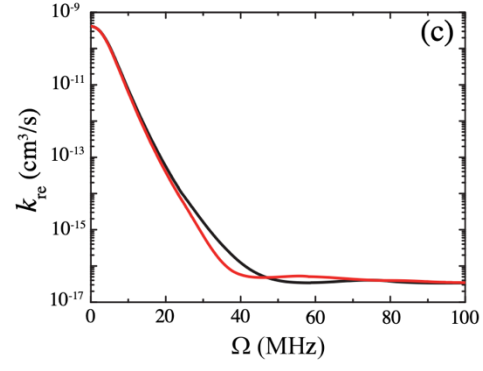
Elastic collisions



Inelastic collisions

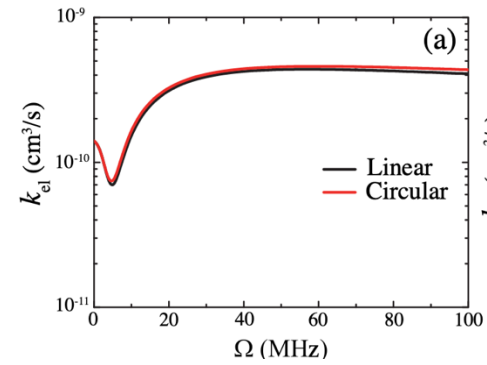


Reactive collisions

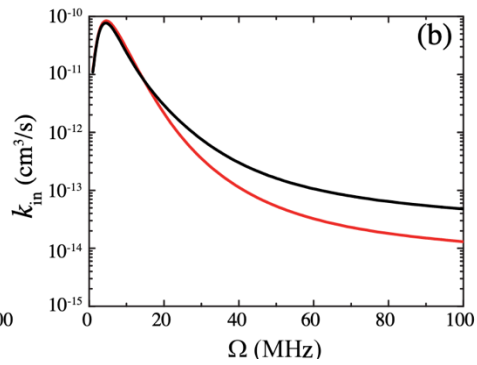


# Results: Optical shielding X.Tie *et al* PRL 125, 153202 (2020)

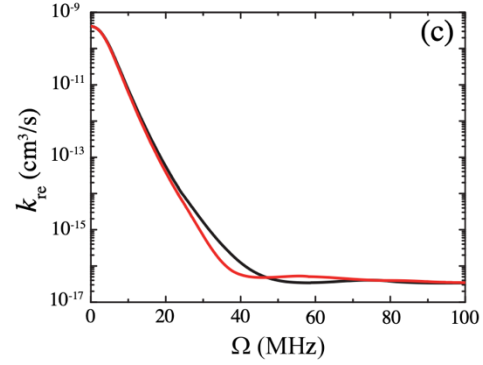
## Elastic collisions



## Inelastic collisions

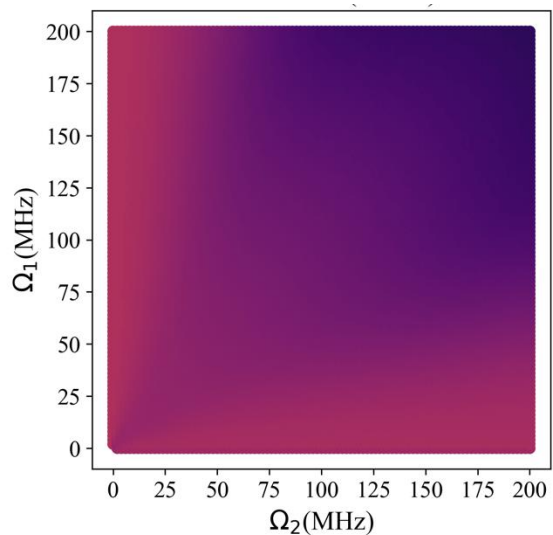


## Reactive collisions

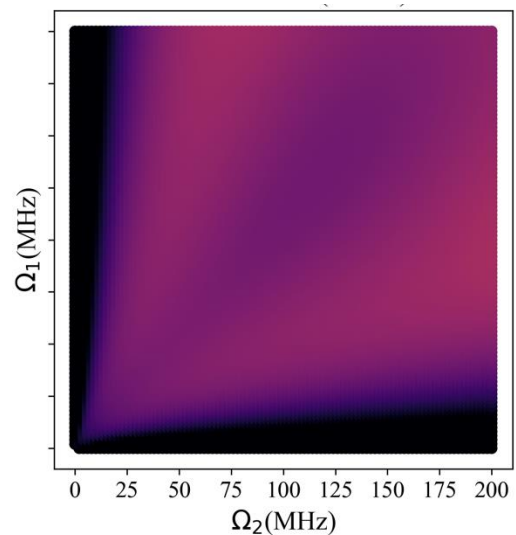


# Results: Two photon optical shielding

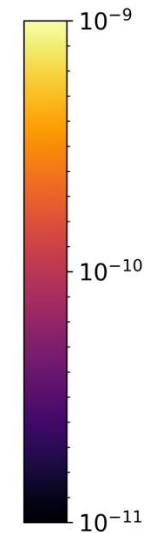
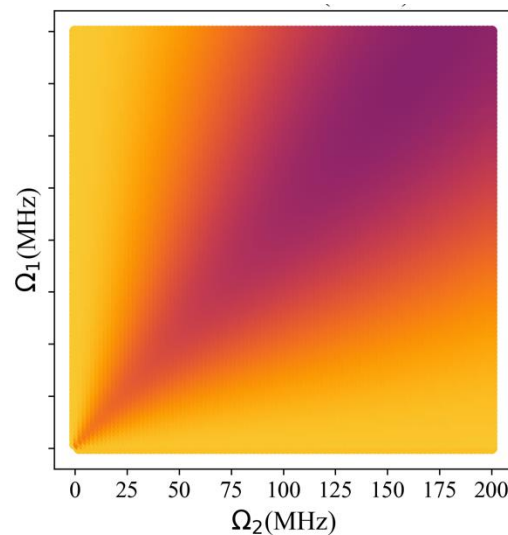
## Elastic collisions



## Inelastic collisions



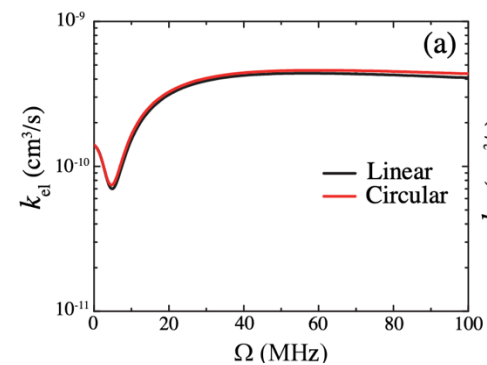
## Reactive collisions



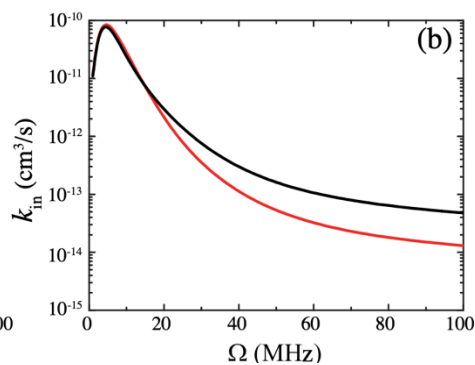
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X.Tie *et al* PRL 125, 153202 (2020)

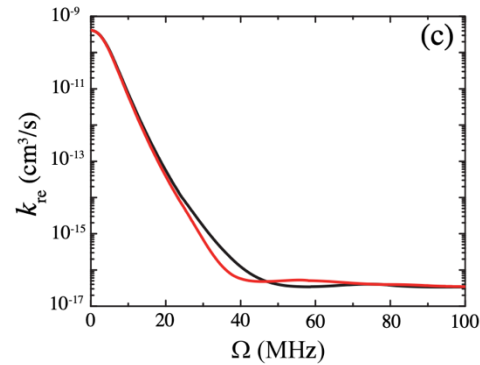
## Elastic collisions



## Inelastic collisions

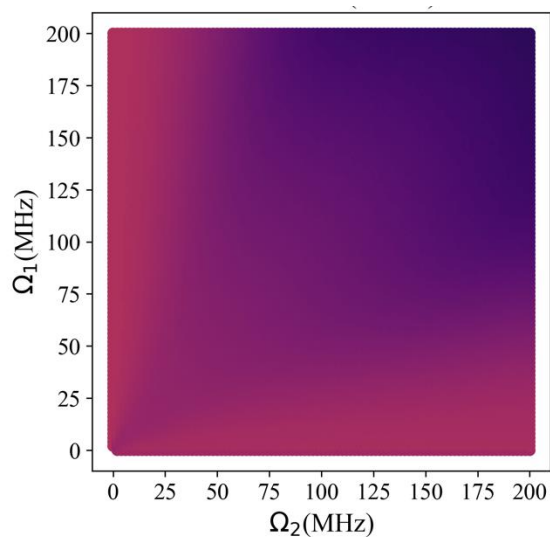


## Reactive collisions

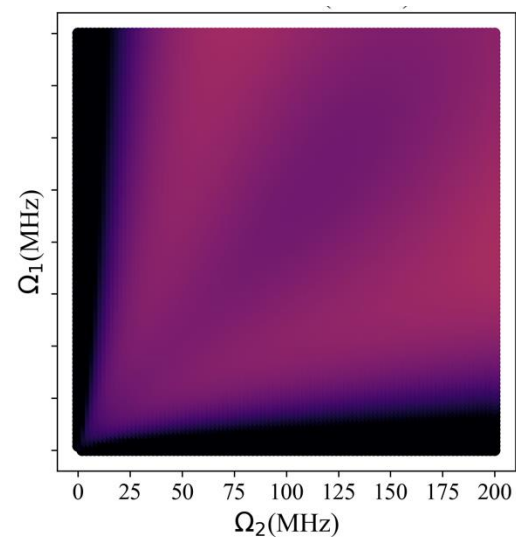


# Results: Two photon optical shielding

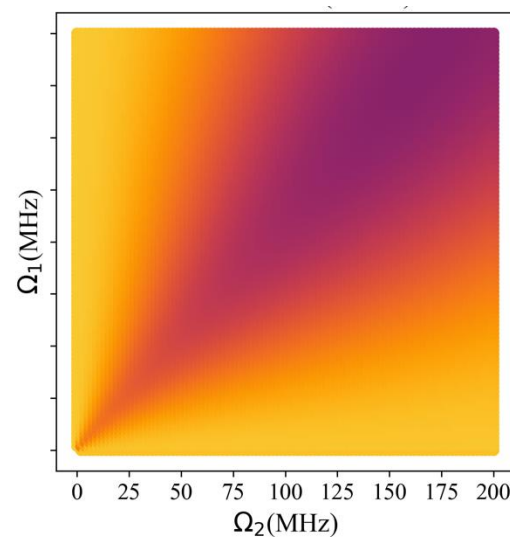
## Elastic collisions



## Inelastic collisions

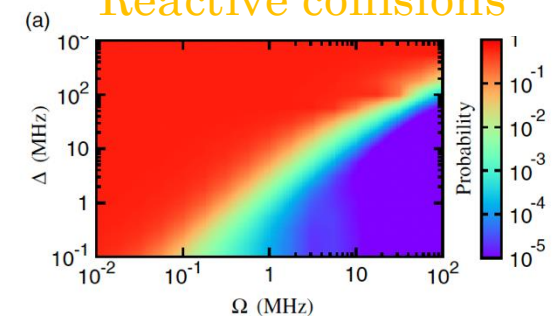


## Reactive collisions

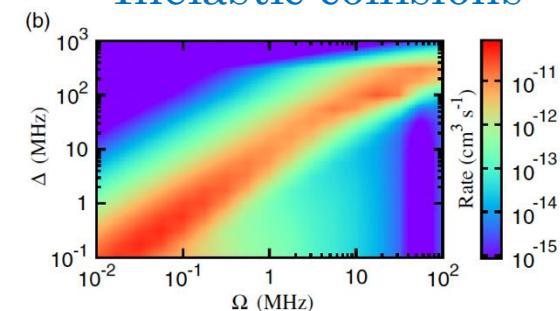


# Results: Microwave shielding

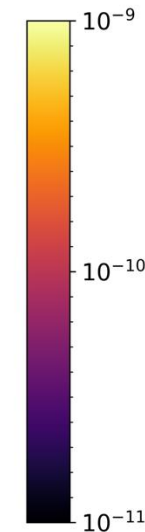
## Reactive collisions



## Inelastic collisions



Karman *et al*  
PRL 121, 163401 (2018)



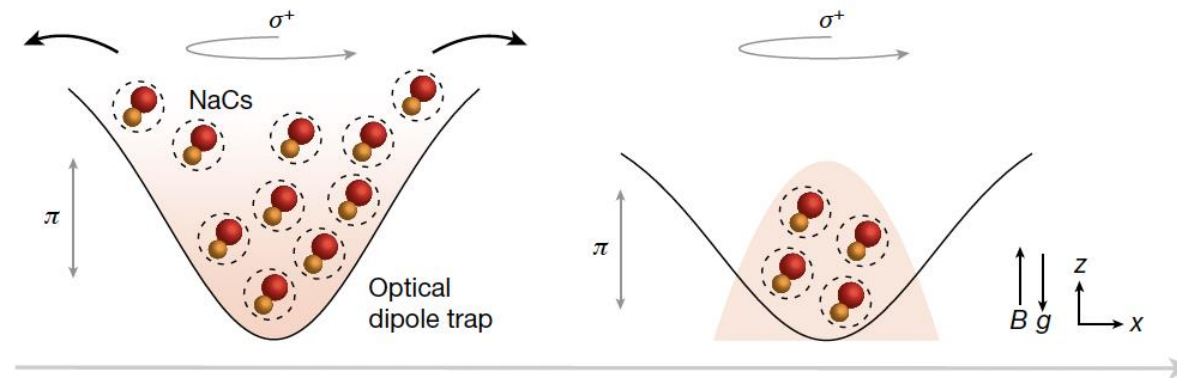
# First observation of ground state molecular BEC

Bigagli *et al* Nature Phys. 19, 1579 (2024)

Step 1:  
Density

Microwave Shielding  $\longrightarrow$  Stable & Good Density

Step 2:  
Temperature  
Evaporative cooling



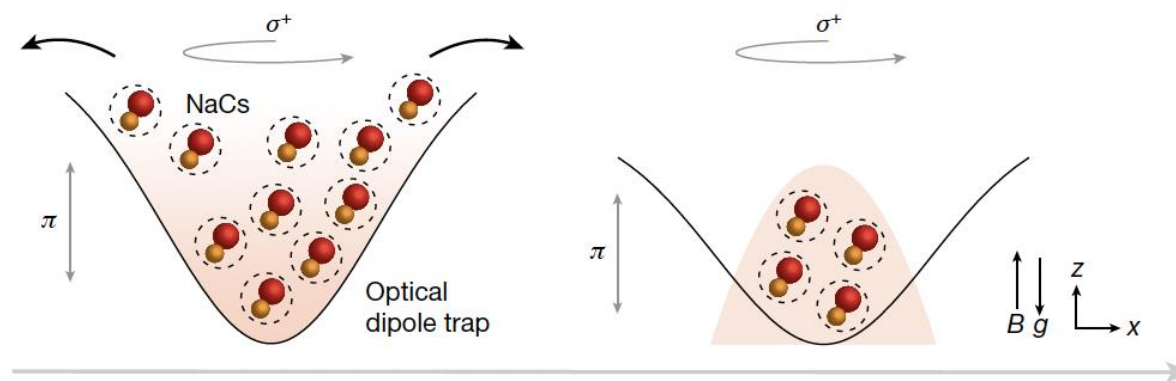
# First observation of ground state molecular BEC

Bigagli *et al* Nature Phys. 19, 1579 (2024)

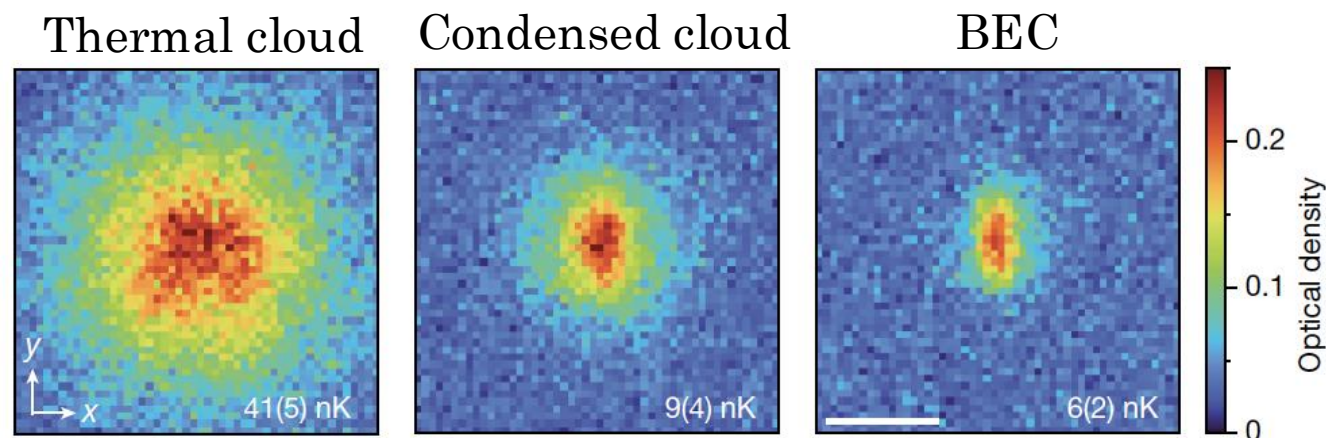
Step 1:  
Density

Microwave Shielding  $\longrightarrow$  Stable & Good Density

Step 2:  
Temperature  
Evaporative cooling



Step 3:

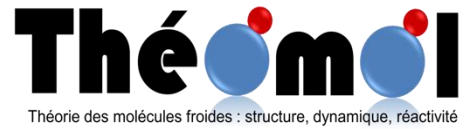




# Conclusion

- ❑ Molecular BEC bring many of the theoretical predictions on dipolar gases into experimental reach.
- ❑ Ground state bi-alkali systems suffer from two-body losses.
- ❑ Shielding allows to engineer the interactions between the molecules to avoid losses.
- ❑ Shielding was experimentally proven to be efficient and lead to the formation of the first BEC of GD molecules.

# Team and collaborators



- Gohar Hovhannesian
- Romain Vexiau
- Maxence Lepers
- Eliane Luc-Koenig
- Goulven Quéméner
- Nadia Bouloufa
- Olivier Dulieu





Thank you!

